

Unit 7: Work, Energy and Power

1 - Work

Energy: the ability to do work

Work and energy are:

Scalar values

Measured in N·m or Joules

Work can be defined as either:

A change in energy or

The product of... force + displacement

$$W = \Delta E$$

$$W = Fd$$

In physics we talk about work being done...

Ex. on an object

- If I hold a 30 kg weight at a height of 1.5 m, I'm using energy, therefore.
- However the work is **not** being done ^{I'm doing work} to the weight, it is being done on my muscles.
- Think of it like this: though I am exerting a force on the weight, its displacement is zero, therefore no work is done on it.

Ex. If I were to lift the 30.0 kg weight up off the ground to a height of 1.5 m, how much work would be done on the weight?

$$m = 30.0 \text{ kg}$$

$$d = 1.5 \text{ m}$$

$$W = mgh$$

$$= (30.0)(9.8)(1.5)$$

$$= 440 \text{ J}$$

When an object is lifted against gravity the formula:

$$W = Fd$$

$$W = mgh$$

Where: m = mass
g = accel due to g
h = height

Ex. A 10.0 kg pumpkin is moved horizontally 5.00 m at a constant velocity across a level floor using a horizontal force of 3.00 N. How much work is done in moving the pumpkin?

m = 10.0 kg
d = 5.00 m
F = 3.00 N

$$W = Fd$$

$$= (3.00)(5.00)$$

$$= 15.0 \text{ J}$$

Note: Use applied force, not net force

Ex. A 3.0 kg pineapple is held 1.2 m above the floor for 15 s. How much work is done on the pineapple?

m = 3.0 kg
h = 1.2 m
t = 15 s

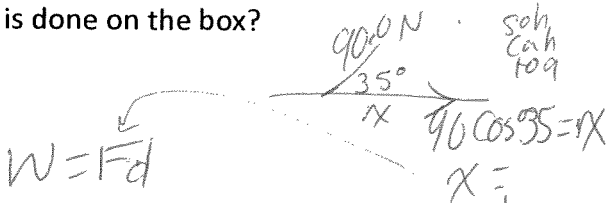
$$W = mgh$$

$$= (3.0)(9.8)(1.2)$$

Note: No displacement means no work done on the object.

Ex. A 50.0 kg banana box is pulled 11.0 m along a level surface by a rope. If the rope makes an angle with the floor of 35° and the tension in the rope is 90.0 N, how much work is done on the box?

m = 50.0 kg
d = 11.0 m



$$W = Fd$$

Note: Use on the ~~only~~ component of the force that is in the direction of displacement

Ex. A 1385 kg car traveling at 61 km/h is brought to a stop while skidding 42 m. What is the work done on the car by frictional forces?

m = 1385 kg
v_i = 61 km/h
v_f = 0
d = 42 m
W = ?

$$F = ma$$

$$W = Fd$$

$$v^2 = v_0^2 + 2ad$$

$$0 = (16.9)^2 + 2a(42)$$

$$a = -1.98 \text{ m/s}^2$$

$$F = 1385(-1.98) = -2.75 \times 10^3 \text{ N}$$

$$W = (-2.75 \times 10^3)(42) = -1.16 \times 10^5 \text{ J}$$

Note: Work can be Negative if the force doing the work acts in the negative direction.

Worksheet 7.1: Work

5. A 20.0 N pomegranate is lifted at a constant velocity from the floor to a height of 1.50 m. How much work is done on the object?

$$W = mgh = (20.0)(9.80)(1.50m) = 294 J = 300 J$$

2. A 15.0 N potato is moved horizontally 3.00 m across a level floor using a horizontal force of 6.00 N. How much work is done on the potato?

$$W = F \times d = (6.00)(3.00) = 18.0 J$$

3. A 2.20 N pear is held 2.20 m above the floor for 10.0 s. How much work is done on the pear?

$$W = F \times d = 0 J$$

4. A 10.0 kg pink grapefruit is accelerated horizontally from rest to a velocity of 11.0 m/s in 5.00 s by a horizontal force. How much work is done on the pink grapefruit assuming no friction?

$$m = 10.0 \text{ kg}$$

$$v_i = 0$$

$$v_f = 11.0 \text{ m/s}$$

$$t = 5.00 \text{ s}$$

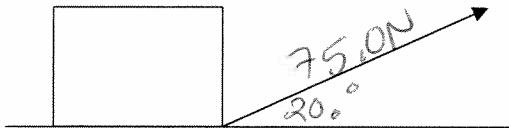
$$d = 27.5$$

$$a = \frac{v^2 - v_0^2}{2d} = \frac{11^2}{2(27.5)} = 2.2 \text{ m/s}^2$$

$$F = ma = (2.2)(10) = 22 \text{ N}$$

$$W = (22 \text{ N})(27.5 \text{ m}) = 605 \text{ J}$$

5. A 90.0 N box of papayas is pulled 10.0 m along a level surface by a rope. If the rope makes an angle of 20.0° with the surface, and the force in the rope is 75.0 N, how much work is done on the box?



$$F_x = 75 \cos 20^\circ = 70.48 \text{ N}$$

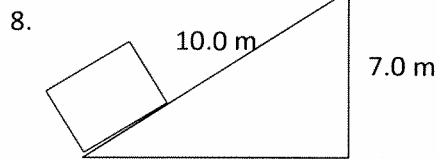
$$W = F_x \times d = (70.48 \text{ N})(10.0 \text{ m}) = 705 \text{ J}$$

6. A 60.0 kg student runs at a constant velocity up a flight of stairs. If the height of the stairs is 3.2 m, what is the work done against gravity?

$$W = mgh = (60.0)(9.80)(3.2) = 1900 \text{ J}$$

7. A 20.0 kg passionfruit is pulled horizontally 9.0 m along a level frictionless surface at a constant velocity. How much work is done on the passionfruit?

$$F = ma, a = 0, F = 0, \therefore W = 0$$



8. An 80.0 kg pumpkin is pushed up at a constant velocity along a frictionless incline as shown in the diagram. How much work is done on the pumpkin in moving it up the incline?

$$W = mgh = (80.0)(9.80)(7.0 \text{ m}) = 5500 \text{ J}$$

9. A 25.0 kg pickle is accelerated from rest through a distance of 6.0 m in 4.0 s across a level floor. If the friction force between the pickle and the floor is 3.8 N, what is the work done to move the object?

$$m = 25.0 \text{ kg}$$

$$d = 6.0 \text{ m}$$

$$t = 4.0 \text{ s}$$

$$v_f = ?$$

$$F_f = 3.8 \text{ N}$$

$$F_{net} = ma$$

$$F_{app} = ma + F_f = (25)(0.75) + 3.8 = 22.55 \text{ N}$$

$$a = \frac{2d - v_0 t^2}{t^2} = \frac{2(6)}{4^2} = 0.75 \text{ m/s}^2$$

$$W = F_{app} \times d = (22.55 \text{ N})(6 \text{ m}) = 135 \text{ J}$$

10. A 1165 kg car traveling at 55 km/h is brought to a stop while skidding 38 m. Calculate the work done on the car by the friction forces.

$$m = 1165 \text{ kg}$$

$$v_i = 15.3 \text{ m/s}$$

$$v_f = 0$$

$$d = -38 \text{ m}$$

$$F = (1165)(3.07) = 3580 \text{ N}$$

$$W = F \times d = (3580 \text{ N})(38 \text{ m}) = 1.35 \times 10^5 \text{ J}$$

$$a = \frac{v^2 - v_0^2}{2d} = \frac{(15.3)^2}{2(-38)} = -3.07 \text{ m/s}^2$$