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## Math 8 Final Exam

## Multiple Choice

Identify the choice that best completes the statement or answers the question.
$\qquad$ 1. Which of these numbers is a perfect square: $50,20,25$, or 15 ?
a. 50
b. 20
c. 25
d. 15
$\qquad$ 2. What is the side length of a square with area $25 \mathrm{~cm}^{2}$ ?
a. 5 cm
b. $\quad 12.5 \mathrm{~cm}$
c. 6.25 cm
d. 20 cm
$\qquad$ 3. Find $8^{2}$.
a. 8
b. 64
c. 16
d. 32
$\qquad$ 4. Which whole number is $\sqrt{8}$ closer to?
a. 5
b. 4
c. 3
d. 2
$\qquad$ 5. The area of square $P$ is $52 \mathrm{~cm}^{2}$.

Square Q has an area equal to one quarter the area of square P .
Find the approximate side length of square Q .
Give your answer to 1 decimal place.
a. $\quad 3.6 \mathrm{~cm}$
b. $\quad 5.1 \mathrm{~cm}$
c. 13 cm
d. $\quad 1.8 \mathrm{~cm}$
$\qquad$ 6. Find the length of the hypotenuse. Give your answer to 1 decimal place.

a. $\quad 144.0$
b. $\quad 10.4$
c. 13.4
d. 36.0
7. The area, in square centimetres, of the square on each side of a triangle is given. Which triangle is NOT a right triangle?

a. Triangle D
b. Triangle C
c. Triangle B
d. Triangle A
8. In a right triangle, the length of the hypotenuse is 18 m and the length of one of the legs is 15 m . Find the length of the other leg. Round your answer to the nearest tenth.
a. $\quad 5.0 \mathrm{~m}$
b. $\quad 6.8 \mathrm{~m}$
c. $\quad 9.9 \mathrm{~m}$
d. 23.4 m
9. This diagram shows 2 flag poles that are 4.5 m tall. The distance from the top of the left pole to the base of the right pole is 7.5 m . What is the distance between the 2 flag poles?

a. $\quad 5.0 \mathrm{~m}$
b. $\quad 6.0 \mathrm{~m}$
c. $\quad 3.0 \mathrm{~m}$
d. 4.5 m
10. Find the product $(+5) \times(-9)$. Use a number line if necessary.
a. -45
b. +45
c. +14
d. -4
11. Replace $\square$ with an integer to make the equation true.
$\square \times(-5)=-30$
a. +6
b. -6
c. -25
d. +25
$\qquad$ 12. Find this product. $(-15) \times(-8)$
a. $\quad-120$
b. +120
c. +23
d. -23
$\qquad$ 13. Find the quotient $(-21) \div(-3)$. Use a number line if it helps.
a. -24
b. -7
c. -18
d. +7
$\qquad$ 14. Evaluate. $9+(-7)-(-4)$
a. 6
b. -2
c. 12
d. 20
$\qquad$ 15. Evaluate. $(-6)[(-3)+9]$
a. 72
b. -36
c. -72
d. 27
$\qquad$ 16. Evaluate. $-13+9 \div(-3)+9$
a. 1
b. -1
c. 7
d. -7
$\qquad$ 17. Multiply. $2 \times \frac{7}{12}$
a. $\frac{7}{24}$
b. $\frac{7}{6}$
c. $\frac{3}{4}$
d. $\frac{31}{12}$
$\qquad$ 18. Find this product. $\frac{4}{5} \times \frac{15}{20}$
a. $\frac{19}{25}$
b. $\frac{2}{3}$
c. $\frac{3}{5}$
d. $\frac{19}{100}$
$\qquad$ 19. Find the reciprocal of $\frac{2}{11}$.
a. $\frac{-11}{2}$
b. $\frac{-2}{-11}$
c. $\frac{-2}{11}$
d. $\frac{11}{2}$
$\qquad$ 20. Write $3 \frac{2}{3}$ as an improper fraction.
a. $\frac{11}{3}$
b. $\frac{5}{3}$
c. $\frac{8}{3}$
d. $\frac{15}{3}$
$\qquad$ 21. Multiply. $1 \frac{1}{3} \times 2 \frac{1}{3}$
a. $3 \frac{1}{9}$
b. $2 \frac{1}{9}$
c. $1 \frac{2}{9}$
d. $3 \frac{2}{3}$
$\qquad$ 22. Find this quotient. $8 \div \frac{1}{3}$
a. 24
b. $2 \frac{2}{3}$
c. $\frac{3}{8}$
d. $\frac{1}{24}$
$\qquad$ 23. Find this quotient. $\frac{8}{12} \div 4$
a. 6
b. $\frac{1}{6}$
c. $\frac{2}{3}$
d. $\frac{8}{3}$
$\qquad$ 24. Find this quotient. $\frac{5}{3} \div \frac{15}{7}$
a. $3 \frac{4}{7}$
b. $\frac{7}{9}$
c. $\frac{7}{15}$
d. $2 \frac{2}{15}$
$\qquad$ 25. Divide. $\frac{4}{5} \div \frac{5}{4}$
a. 1
b. $\frac{16}{25}$
c. $1 \frac{9}{16}$
d. $\frac{8}{25}$
$\qquad$ 26. Divide. $2 \frac{1}{3} \div 2 \frac{1}{2}$
a. $\frac{14}{15}$
b. $5 \frac{5}{6}$
c. $\frac{2}{3}$
d. $1 \frac{1}{14}$
$\qquad$ 27. Which operation would you do first?
$\frac{5}{6} \times\left(\frac{6}{7}+\frac{7}{8}\right) \div \frac{8}{7}-\frac{5}{6}$
a. Addition
b. Subtraction
c. Multiplication
d. Division
$\qquad$ 28. Which operation would you do first?
$\left(\frac{5}{6}-\frac{7}{8}\right) \times \frac{6}{7} \div \frac{5}{6}+\frac{6}{5}$
a. Addition
b. Subtraction
c. Multiplication
d. Division
29. Evaluate. $\frac{2}{3}+\frac{3}{5} \times \frac{15}{4}$
a. $2 \frac{11}{12}$
b. $4 \frac{3}{4}$
c. $1 \frac{1}{4}$
d. $2 \frac{1}{12}$
$\qquad$ 30. This is an incomplete net for a triangular prism. What shapes do you add to complete this net?

a. 3 squares
b. 1 triangle and 2 squares
c. 1 triangle and 3 squares
d. 3 triangles
$\qquad$ 31. Which diagram is the net for a square pyramid?

a. Net A
b. Net B
c. Net C
d. Net D
32. Name the polyhedron that can be made from this net.

a. Rectangular pyramid
c. Rectangular prism
b. Triangular prism
d. Triangular pyramid
$\qquad$ 33. How many triangular faces are there in a pentagonal pyramid?
a. 1
b. 5
c. 2
d. 3
$\qquad$ 34. Find the surface area of this right rectangular prism.

a. $420 \mathrm{~m}^{2}$
b. $\quad 300 \mathrm{~m}^{2}$
c. $600 \mathrm{~m}^{2}$
d. $480 \mathrm{~m}^{2}$
$\qquad$ 35. Use the net to find the surface area of the right triangular prism.

a. $\quad 90 \mathrm{~m}^{2}$
b. $585 \mathrm{~m}^{2}$
c. $510 \mathrm{~m}^{2}$
d. $\quad 2340 \mathrm{~m}^{2}$
$\qquad$ 36. A right rectangular prism measures 9 cm by 7 cm by 10 cm . What is the volume of the prism?
a. $\quad 630 \mathrm{~cm}^{3}$
b. $\quad 104 \mathrm{~cm}^{3}$
c. $223 \mathrm{~cm}^{3}$
d. $\quad 156 \mathrm{~cm}^{3}$
37. Find the volume of this triangular prism.

a. $\quad 160 \mathrm{~m}^{3}$
b. $80 \mathrm{~m}^{3}$
c. $320 \mathrm{~m}^{3}$
d. $184 \mathrm{~m}^{3}$
$\qquad$ 38. Find the surface area of this cylinder to the nearest square metre.

a. $\quad 905 \mathrm{~m}^{2}$
b. $\quad 704 \mathrm{~m}^{2}$
c. $653 \mathrm{~m}^{2}$
d. $452 \mathrm{~m}^{2}$
39. Find the volume of this cylinder. Round your answer to the nearest tenth.

a. $\quad 747.7 \mathrm{~m}^{3}$
b. $\quad 373.8 \mathrm{~m}^{3}$
c. $\quad 2616.9 \mathrm{~m}^{3}$
d. $238 \mathrm{~m}^{3}$
$\qquad$ 40. Write $76 \%$ as a decimal.
a. 7.6
b. 0.76
c. 0.076
d. 76
$\qquad$ 41. Write this fraction as a percent.
$\frac{659}{100}$
a. $659 \%$
b. $653 \%$
c. $6.59 \%$
d. $6.57 \%$
$\qquad$ 42. Find $274 \%$ of 70 .
a. $\quad 39.14$
b. 1918
c. $\quad 19.18$
d. 191.8
$\qquad$ 43. Calculate the sale price of this item before taxes.
$30 \%$ off a bike for $\$ 397.95$
a. $\$ 179.08$
b. $\$ 119.39$
c. $\$ 238.77$
d. $\$ 278.57$
$\qquad$ 44. The sales taxes are $14 \%$. Find the tax paid for a pair of running shoes that costs $\$ 115$.
a. $\quad \$ 16.10$
b. $\$ 161.00$
c. $\$ 1.22$
d. $\$ 2.25$
$\qquad$ 45. What is the ratio of triangles to circles?

a. $6: 5$
b. $5: 6$
c. $7: 5$
d. $5: 7$
$\qquad$ 46. The ratio of boys to girls in a class is 5 to 6 .

What is the ratio of boys to students in the class?
a. 6 to 30
b. 6 to 11
c. 5 to 30
d. 5 to 11
$\qquad$ 47. The ratios $40: \square$ and $8: 7$ are equivalent. Find the missing number.
a. 42
b. 35
c. 32
d. 55
$\qquad$ 48. Find the value of the variable.
$18: 12=30: w$
a. 28
b. 40
c. 56
d. 20
$\qquad$ 49. One hundred nautical miles is about 185 km .

About how many kilometres is 120 nautical miles?
a. $\quad 65 \mathrm{~km}$
b. 222 km
c. $\quad 185 \mathrm{~km}$
d. 2220 km
$\qquad$ 50. At the market, 5 cans of soup cost $\$ 4.75$. What is the cost of 1 can of soup?
a. $97 \varnothing$
b. $\$ 1.90$
c. $96 \notin$
d. $95 \phi$
$\qquad$ 51. You pay $\$ 2.80$ for 7 bagels. Find the unit cost for these bagels.
a. $\quad \$ 0.47$ per bagel
b. $\$ 0.40$ per bagel
c. $\$ 0.50$ per bagel
d. $\$ 0.20$ per bagel
$\qquad$ 52. Use this balance-scales model to solve for $x$.

a. $\quad-4$
b. 9
c. 15
d. 4
$\qquad$ 53. Solve this equation. $3 x+11=23$
a. 9
b. 4
c. 11
d. -4
$\qquad$ 54. Write an equation for this situation.

Patricia has $p$ posters. She sold 8 and has 18 left.
a. $p+18=8$
b. $p-8=18$
c. $p+8=18$
d. $p=18-8$
$\qquad$ 55. Solve this equation. $4 y+8=36$
a. 1
b. 3
c. 7
d. 24
$\qquad$ 56. Solve this equation. $\frac{x}{-6}=-9$
a. 54
b. -54
c. -15
d. -3
$\qquad$ 57. Solve this equation. $9+\frac{d}{4}=23$
a. 83
b. -13
c. 56
d. 10
$\qquad$ 58. Solve this equation. $\frac{t}{-2}-7=16$
a. $\quad-46$
b. -25
c. 30
d. 21
$\qquad$ 59. Expand. $4(x+7)$
a. $4 x+7$
b. $4 x+28$
c. $4+x+7$
d. $28 x$
$\qquad$ 60. Expand. $-6(5-x)$
a. $-30+6 x$
b. $-30-6 x$
c. $-11-6 x$
d. $-30-x$
$\qquad$ 61. Solve this equation: $-5(a+4)=15$
a. 1
b. -7
c. 40
d. 7
$\qquad$ 62. The ordered pair $(5$,$) is in the linear relation with equation y=-2 x+8$.

Find the missing number in the ordered pair.
a. 1
b. 11
c. -2
d. -18
$\qquad$ 63. Graph the relation $y=-2 x+3$ for integer values of $x$ from 0 to 4 .
a.

c.

b.

d.

64. Which relations have graphs that are lines going up to the right?
i) $y=-5 x+3$
ii) $y=5 x+3$
iii) $y=-5 x-3$
iv) $y=5 x-3$
a. ii and iv
b. i and iii
c. ii
d. i, ii, and iv
65. This graph shows the number of customers buying from a store in September and October.


Is the graph misleading? If it is misleading, explain why.
a. Yes, the bars do not touch.
b. No, the graph is not misleading.
c. Yes, the intervals on the vertical axis between 200 and 207 are not even.
d. Yes, the graph exaggerates the difference in the number of customers between September and October.
$\qquad$ 66. A clothing manufacturer offers 2 different styles of jeans, relaxed fit and regular fit, in 5 different colours. How many combinations of a style and a colour are possible?
a. 4
b. 8
c. 7
d. 10
$\qquad$ 67. A coin is tossed and a regular 6 -sided die labelled 1 to 6 is rolled.

What is the probability of tossing a head and rolling a 5 ?
a. $\frac{1}{12}$
b. $\frac{1}{4}$
c. $\frac{2}{3}$
d. $\frac{1}{6}$
$\qquad$ 68. A red die, a blue die, and a green die are rolled. Each is a regular 6-sided die labelled 1 to 6 . What is the probability of rolling an even number on each die?
a. $\frac{1}{6}$
b. $\frac{1}{216}$
c. $\frac{1}{2}$
d. $\frac{1}{8}$
69. This object is made using 4 linking cubes. Draw the right side view of the object.

a.

b.

c.

d.

70. Draw the side view of this object.

a.

b.

c.

d.

71. This object is built using 4 linking cubes.

The object is rotated vertically $90^{\circ}$ clockwise about the axis shown.
Draw the right side view of the object after the rotation.

a.

b.

c.

d.

$\qquad$ 72. This object is built using 7 linking cubes.

The object is rotated vertically $90^{\circ}$ clockwise about the axis shown.


Which view is the front view of the object after the rotation?


View K
b. View L



View M


View N
a. View K
c. View M
d. View N
73. These are views of an object built using linking cubes. Sketch the object.

a.

b.

c.

d.

$\qquad$ 74. These are views of an object built using linking cubes. Sketch the object.

a.

c.

b.

d.

75. These are views of an object built using linking cubes.

The letters refer to the colours of the cubes.
$\mathrm{R}=$ red, $\mathrm{B}=$ blue, $\mathrm{G}=$ green, $\mathrm{Y}=$ yellow, and $\mathrm{P}=$ purple Sketch the object and label the colours.

$$
\begin{aligned}
& \text { Top view } \\
& \begin{array}{|l|l|l|}
\hline \mathrm{R} & \mathrm{~B} & \mathrm{P} \\
\hline
\end{array}
\end{aligned}
$$



Left side view Front view Right side view
a.

b.

c.

d.

$\qquad$ 76. Triangle B is a translation image of Triangle A. Describe the translation.

a. 5 units right and 3 units down
b. 5 units left and 3 units up
c. 3 units right and 5 units down
d. 3 units left and 5 units up
77. Triangle B is the image of Triangle A after a reflection in a vertical line through the point $(6,0)$. Which diagram shows the correct position of Triangle B?
a.

c.

b.

d.

$\qquad$ 78. Triangle SOQ is a transformation image of Triangle KOV. Describe the transformation.

a. $90^{\circ}$ clockwise rotation about O
b. Reflection in the line PT
c. $180^{\circ}$ rotation about O
d. Translation 4 units right and 2 units down
$\qquad$ 79. Which shape does not tessellate?


a. Shape A
c. Shape C
d. Shape D
$\qquad$ 80. This L-shape below is used to create the design on its right.


Identify the transformations used.
a. Translations only
b. Reflections only
c. Rotations only
d. None of these

## Short Answer

81. Order from least to greatest: $5^{2}, 4^{2}, \sqrt{289}, 19$
82. What is a factor?
83. This logo is made up of 4 congruent right triangles. Find the perimeter of the logo.

84. Write the next 2 terms in this pattern. Then write a pattern rule.
$+2,-6,+18,-54, \ldots$.
85. The water level in a pool dropped 80 mm each hour. The total drop in water level was 480 mm . How long did it take for the water level to change?
86. Find $\frac{2}{3}$ of $\frac{4}{7}$.
87. Find this product. $\frac{3}{8} \times \frac{20}{21}$
88. Evaluate. $\sqrt{\frac{25}{36}}$
89. Write the mixed number and the improper fraction represented by this picture.

90. Write the reciprocal of $2 \frac{3}{4}$.
91. Write $\frac{41}{4}$ as a mixed number.
92. Evaluate. $2 \frac{7}{10} \times 1 \frac{1}{4} \div 3 \frac{3}{8}$
93. Sketch a net for each object.
a) a closed cylinder
b) an open cylinder
94. The surface area of a cube is $216 \mathrm{~cm}^{2}$.
a) What is the surface area of one face of the cube?
b) What is the length of one edge of the cube?
95. The 2 ends of a right triangular prism are equilateral triangles. Each has an area of $27 \mathrm{~cm}^{2}$. The total surface area of the prism is $390 \mathrm{~cm}^{2}$. Calculate the area of each rectangular face.
96. If each of the length, width, and height of a rectangular prism is doubled, what happens to the volume?
97. Calculate the volume of this triangular prism.

98. A circle has radius 18 cm . Find the circumference to the nearest centimetre.
99. There are 26 concrete cylindrical pillars in a stadium.

Each column has diameter 3.4 m and height 12 m .
Calculate the total volume of concrete in the pillars, to the nearest cubic metre. Use $\pi=3.14$.
100. Write $\frac{18}{240}$ as a decimal and as a percent.
101. What percent of 200 is 69 ?
102. You have 4 red cubes, 5 blue cubes, and 7 green cubes.

Which sets of cubes could you use to show the ratio 7:9?
103. Write 2 ratios equivalent to the ratio 5:2.
104. Miguel made 5 of 12 free shots in his basketball game.

Nadia made 8 of 11 free shots in her basketball game.
Who played better? Explain.
105. What is the mass needed to balance these scales?

106. A white square represents +1 , a black square represents -1 , and a black rectangle represents $-x$. Find the value of $x$.

107. Solve this equation. $-6 p+9=-33$
108. Solve this equation: $5(y-6)=10$
109. Make a table of values for the relation $y=x-4$ for $x=-4,-3,-2,-1,0$.
110. This table of values is for the linear relation with equation $y=b-x$, where $b$ is a constant. Find the value of $b$.

| $x$ | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 11 | 10 | 9 | 8 | 7 |

111. Two regular 6 -sided dice, each labelled 1 to 6 , are rolled. What is the probability of rolling 2 even numbers?
112. A yellow die, a purple die, and a green die are rolled. Each is a regular 8 -sided die labelled 1 to 8 . What is the probability of rolling a 4 on the yellow die, a 2 on the purple die, and a 7 on the green die?
113. There are 3 decks of standard playing cards. Each of 3 students picks a card at random from a deck. What is the probability of each student picking a face card (Jack, Queen, King)?
114. This object is made using linking cubes. Sketch the right side, front, and top views of the object.

115. This object is built using 8 linking cubes.

The object is rotated vertically $90^{\circ}$ away from you about the horizontal axis shown. Draw the top, front, and side views of the rotated object.

116. These are the views of an object built using linking cubes. Use these views to build the object.

117. Use this diagram to identify each transformation.

a) Triangle $R$ is the image of Triangle $V$.
b) Triangle R is the image of Triangle P .
118. Create a design by applying each transformation to the original shape.

a) Reflection in Line $m$
b) $180^{\circ}$ rotation about point O
c) Reflection in Line 1
119. Jodi wants to tile her bedroom floor with octagons. This pattern shows part of the floor.


Does Jodi need another shape to cover the floor with no gaps? If so, what is it?
120. Draw the 4th tile in this tessellation.


## Problem

121. A square and a rectangle have the same area.

The rectangle has length 9 cm and height 16 cm .
Find the area and perimeter of the square.
122. The length of the hypotenuse of a right triangle is $\sqrt{10} \mathrm{~cm}$.

Give 3 possible lengths of the legs of the triangle.
123. In this diagram, $\mathrm{PT}=\mathrm{RT}$. Find the measure of ST . Show your work.

Give your answer to 1 decimal place.

124. Sarah says triangle ABC is a right triangle.

Is she correct? Justify your answer.

125. Find the length of BC to the nearest tenth. Show your work.

126. Explain how you could predict the sign of the product $(-8)(+9)(+7)(-4)$ without actually multiplying.
127. Find all the integers that divide -22 exactly. Show your work.
128. In a darts game, Jamie and Corinne each threw 10 darts.

Jamie had three $(+6)$ scores, four $(+7)$ scores, and three $(-8)$ scores.
Corinne had five ( +6 ) scores, two $(+7)$ scores, and three ( -8 ) scores.
a) What were the final scores for Jamie and Corinne? Show your work.
b) If the winner was the one with the greater score, who won?
129. Multiply $4 \frac{4}{5} \times 6 \frac{1}{4} \times \frac{7}{20}$. Show your work.
130. Evaluate. Show your steps.
$\sqrt{5 \frac{1}{4} \div 1 \frac{5}{7}}$
131. Which object has the greater surface area?

- A cylinder with radius 3 cm and length 8 cm
- A cube of edge length 6 cm

Explain.
132. An immunization program claims that $99.75 \%$ of those vaccinated are safe from a virus. If 564000 children were vaccinated, about how many are still at risk? Show your work.
133. A bag contains 234 red cubes and green cubes in the ratio of 6 red to 7 green.

How many of each colour are there in the bag? Explain your strategy.
134. In 3 stores, the same detergent is on special. Which store offers the best buy? Explain.

A: 6 bottles for $\$ 12.48$
B: 7 bottles for $\$ 14.42$
C: 5 bottles for $\$ 10.35$
135. Use this balance-scales model to solve for $x$. Show your work.

136. a) Graph both relations on the same coordinate axes.
i) $y=8-x$
ii) $y=x+2$
b) Find the ordered pair on the graph that are in both relations.
137. Victor has 20 songs on a CD. The songs are: 4 by group $A, 6$ by group $B, 3$ by group $C$, and 7 by group D. He selects a setting that randomly chooses songs to play.
Find the probability of each event.
a) The first 3 songs played are by group A .
b) The first song played is by group $B$, and the next 2 songs are by group $D$.
c) The first 3 songs played are not by group A.

Show your work.
138. Draw the image of Shape $A$ after a reflection in the diagonal Line $m$.

139. In this tessellation, Triangle Q is the image of Triangle P .


Describe possible combinations of transformations you can use to transform Triangle P to Triangle Q.

## Math 8 Final Exam

Answer Section

## MULTIPLE CHOICE







## SHORT ANSWER

81. ANS:
$4^{2}, \sqrt{289}, 19,5^{2}$

PTS: 1 DIF: Moderate REF: 1.2 Squares and Square Roots
LOC: 8.N1 TOP: Number KEY: Conceptual Understanding
82. ANS:

A factor is a number that divides exactly into another number.
PTS: 1 DIF: Moderate REF: 1.2 Squares and Square Roots
LOC: 8.N1 TOP: Number KEY: Conceptual Understanding
83. ANS:

24 units

PTS: 1 DIF: Moderate REF: 1.7 Applying the Pythagorean Theorem
LOC: 8.SS1 TOP: Shape and Space (Measurement) KEY: Conceptual Understanding
84. ANS:

The next 2 terms are: $+162,-486$
Start at +2 . Multiply by -3 each time.
PTS: 1 DIF: Moderate REF: 2.2 Developing Rules to Multiply Integers
LOC: 8.N7 TOP: Number KEY: Communication | Problem-solving Skills
85. ANS:

6 h

PTS: 1
DIF: Moderate
REF: 2.3 Using Models to Divide Integers
LOC: 8.N7
TOP: Number
KEY: Conceptual Understanding | Problem-solving Skills
86. ANS:
$\frac{8}{21}$

PTS: 1
DIF: Moderate
REF: 3.2 Using Models to Multiply Fractions
LOC: 8.N6
TOP: Number
KEY: Conceptual Understanding
87. ANS:
$\frac{5}{14}$

PTS: 1
DIF: Moderate
REF: 3.3 Multiplying Fractions
LOC: 8.N6
TOP: Number
KEY: Conceptual Understanding
88. ANS:
$\frac{5}{6}$

PTS: 1
LOC: 8.N6
DIF: Moderate
REF: 3.3 Multiplying Fractions
TOP: Number
KEY: Conceptual Understanding | Procedural Knowledge
89. ANS:
$2 \frac{7}{8}, \frac{23}{8}$

PTS: 1 DIF: Easy REF: 3.4 Multiplying Mixed Numbers
LOC: 8.N6
TOP: Number
KEY: Communication
90. ANS:
$\frac{4}{11}$

PTS: 1 DIF: Easy REF: 3.6 Dividing Fractions
LOC: 8.N6
TOP: Number
KEY: Conceptual Understanding
91. ANS:
$10 \frac{1}{4}$

PTS: 1 DIF: Easy REF: 3.7 Dividing Mixed Numbers
LOC: 8.N6 TOP: Number KEY: Conceptual Understanding
92. ANS:

1

PTS: 1 DIF: Difficult REF: 3.7 Dividing Mixed Numbers
LOC: 8.N6 TOP: Number KEY: Conceptual Understanding | Procedural Knowledge
93. ANS:
a) Diagrams may vary. Sample:

b) Diagrams may vary. Sample:


PTS: 1 DIF: Moderate REF: 4.1 Exploring Nets
LOC: 8.SS2 TOP: Shape and Space (Measurement)
KEY: Procedural Knowledge | Communication
94. ANS:
a) $36 \mathrm{~cm}^{2}$
b) 6 cm

PTS: 1 DIF: Moderate REF: 4.3 Surface Area of a Right Rectangular Prism
LOC: 8.SS3 TOP: Shape and Space (Measurement)
KEY: Conceptual Understanding | Problem-solving Skills
95. ANS:

The area of each rectangular face is $112 \mathrm{~cm}^{2}$.

PTS: 1 DIF: Moderate REF: 4.4 Surface Area of a Right Triangular Prism
LOC: 8.SS3 TOP: Shape and Space (Measurement) KEY: Conceptual Understanding
96. ANS:

The new volume equals the original volume multiplied by 8 .

PTS: 1 DIF: Difficult REF: 4.5 Volume of a Right Rectangular Prism
LOC: 8.SS4 TOP: Shape and Space (Measurement)
KEY: Communication | Problem-solving Skills
97. ANS:

The volume of the prism is $220 \mathrm{~cm}^{3}$.
PTS: 1 DIF: Easy REF: 4.6 Volume of a Right Triangular Prism
LOC: 8.SS4 TOP: Shape and Space (Measurement) KEY: Conceptual Understanding
98. ANS:

The circumference of the circle is about 113 cm .

PTS: 1 DIF: Easy REF: 4.7 Surface Area of a Right Cylinder
LOC: 8.SS3 TOP: Shape and Space (Measurement) KEY: Conceptual Understanding
99. ANS:

The volume of concrete in the pillars is about $2831 \mathrm{~m}^{3}$.
PTS: 1 DIF: Moderate REF: 4.8 Volume of a Right Cylinder
LOC: 8.SS4 TOP: Shape and Space (Measurement)
KEY: Conceptual Understanding | Problem-solving Skills
100. ANS:
0.075; 7.5\%

PTS: 1 DIF: Moderate REF: 5.1 Relating Fractions, Decimals, and Percents
LOC: 8.N3 TOP: Number KEY: Conceptual Understanding
101. ANS:

69 is $34.5 \%$ of 200 .

PTS: 1 DIF: Easy REF: 5.3 Solving Percent Problems
LOC: 8.N3 TOP: Number KEY: Conceptual Understanding
102. ANS:

Green to red and blue
PTS: 1
DIF: Moderate
REF: 5.5 Exploring Ratios
LOC: 8.N5
TOP: Number
KEY: Conceptual Understanding | Problem-solving Skills
103. ANS:

Answers may vary. Sample:
The equivalent ratios are 10:4 and 15:6.
PTS: 1 DIF: Easy REF: 5.6 Equivalent Ratios
LOC: 8.N5 TOP: Number KEY: Conceptual Understanding
104. ANS:

Nadia played better.
Miguel: 5:12 $=55: 132$
Nadia: $8: 11=96: 132$
The ratio $5: 12$ is less than the ratio $8: 11$.
PTS: 1 DIF: Moderate REF: 5.7 Comparing Ratios
LOC: 8.N5 TOP: Number KEY: Conceptual Understanding | Communication
105. ANS:

A mass of 11 g is needed for the left pan.
PTS: 1 DIF: Moderate REF: 6.1 Solving Equations Using Models
LOC: 8.PR2 TOP: Patterns and Relations (Variables and Equations)
KEY: Conceptual Understanding
106. ANS:
$x=-2$

PTS: 1 DIF: Moderate REF: 6.1 Solving Equations Using Models
LOC: 8.PR2 TOP: Patterns and Relations (Variables and Equations)
KEY: Conceptual Understanding
107. ANS:
$p=7$

PTS: 1 DIF: Moderate REF: 6.2 Solving Equations Using Algebra
LOC: 8.PR2 TOP: Patterns and Relations (Variables and Equations)
KEY: Conceptual Understanding
108. ANS:
$y=8$

PTS: 1 DIF: Easy
REF: 6.5 Solving Equations Involving the Distributive Property
LOC: 8.PR2 TOP: Patterns and Relations (Variables and Equations)
KEY: Conceptual Understanding
109. ANS:

| $x$ | -4 | -3 | -2 | -1 | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | -8 | -7 | -6 | -5 | -4 |

PTS: 1 DIF: Moderate REF: 6.6 Creating a Table of Values
LOC: 8.PR1 TOP: Patterns and Relations (Patterns) KEY: Conceptual Understanding
110. ANS:
$b=12$

PTS: 1 DIF: Difficult REF: 6.6 Creating a Table of Values
LOC: 8.PR1 TOP: Patterns and Relations (Patterns) KEY: Problem-solving Skills
111. ANS:
$P($ even and even $)=\frac{1}{4}$.

PTS: 1 DIF: Easy REF: 7.3 Probability of Independent Events
LOC: 8.SP2 TOP: Statistics and Probability (Chance and Uncertainty)
KEY: Conceptual Understanding
112. ANS:
$\mathrm{P}(4$ on yellow, 2 on purple, and 7 on green $)=\frac{1}{512}$

PTS: 1 DIF: Moderate REF: 7.4 Solving Problems Involving Independent Events
LOC: 8.SP2 TOP: Statistics and Probability (Chance and Uncertainty)
KEY: Conceptual Understanding
113. ANS:
$\mathrm{P}(3$ face cards in a row $)=\frac{27}{2197}$

PTS: 1 DIF: Moderate REF: 7.4 Solving Problems Involving Independent Events
LOC: 8.SP2 TOP: Statistics and Probability (Chance and Uncertainty)
KEY: Conceptual Understanding
114. ANS:


PTS: 1 DIF: Easy REF: 8.1 Sketching Views of Objects
LOC: 8.SS5 TOP: Shape and Space (3-D Objects and 2-D Shapes)
KEY: Conceptual Understanding | Communication
115. ANS:


PTS: 1 DIF: Difficult REF: 8.2 Drawing Views of Rotated Objects
LOC: 8.SS5 TOP: Shape and Space (3-D Objects and 2-D Shapes)
KEY: Conceptual Understanding | Communication
116. ANS:


PTS: 1 DIF: Moderate REF: 8.3 Building Objects from Their Views
LOC: 8.SS5 TOP: Shape and Space (3-D Objects and 2-D Shapes)
KEY: Communication | Problem-solving Skills
117. ANS:
a) $90^{\circ}$ counterclockwise rotation about the vertex the triangles share.
b) Translation 2 units right and 2 units down.

PTS: 1 DIF: Moderate REF: 8.4 Identifying Transformations
LOC: 8.SS6 TOP: Shape and Space (Transformations)
KEY: Conceptual Understanding | Communication
118. ANS:


PTS: 1 DIF: Moderate REF: 8.4 Identifying Transformations
LOC: 8.SS6 TOP: Shape and Space (Transformations)
KEY: Conceptual Understanding | Communication
119. ANS:

A square

PTS: 1 DIF: Easy REF: 8.5 Constructing Tessellations
LOC: 8.SS6 TOP: Shape and Space (Transformations)
KEY: Conceptual Understanding | Problem-solving Skills
120. ANS:


PTS: 1
DIF: Moderate REF: 8.5 Constructing Tessellations
LOC: 8.SS6
TOP: Shape and Space (Transformations)
KEY: Conceptual Understanding | Communication

## PROBLEM

121. ANS:

Find the area of the square:
The area of the square is the same as the area of the rectangle.
The area of the rectangle is: $9 \times 16=144 \mathrm{~cm}^{2}$
So, the area of the square is $144 \mathrm{~cm}^{2}$.

Find the side length of the square:

Find a number which, when multiplied by itself, gives 144 .
$12 \times 12=144$
So, the square has side length 12 cm .

Perimeter is the distance around the square.
So, $P=12 \mathrm{~cm}+12 \mathrm{~cm}+12 \mathrm{~cm}+12 \mathrm{~cm}$
$=48 \mathrm{~cm}$
The perimeter of the square is 48 cm .

PTS: 1 DIF: Difficult REF: 1.1 Square Numbers and Area Models
LOC: 8.N1 TOP: Number
KEY: Procedural Knowledge | Communication | Problem-solving Skills
122. ANS:

Sample answer:
Find 3 pairs of numbers whose sum is $10: 1$ and 9,2 and 8,3 and 7
So, three possible lengths of the legs are: 1 and $3, \sqrt{2}$ and $\sqrt{8}, \sqrt{3}$ and $\sqrt{7}$

PTS: 1 DIF: Moderate REF: 1.5 The Pythagorean Theorem
LOC: 8.N1|8.SS1 TOP: Number | Shape and Space (Measurement)
KEY: Problem-solving Skills
123. ANS:

Methods may vary. Sample:

$$
\begin{aligned}
\mathrm{PR}^{2}+\mathrm{QR}^{2} & =\mathrm{PQ}^{2} \\
\mathrm{PR}^{2}+5^{2} & =13^{2} \\
\mathrm{PR}^{2} & =13^{2}-5^{2} \\
& =144 \\
\mathrm{PR} & =\sqrt{144} \\
& =12 \\
\mathrm{RT}=\frac{1}{2} \mathrm{PR} & \\
= & \frac{1}{2} \times 12 \\
= & 6 \\
\mathrm{ST}^{2}= & \mathrm{RS}^{2}+\mathrm{RT}^{2} \\
= & 5^{2}+6^{2} \\
& =61 \\
\mathrm{ST} & =\sqrt{61} \\
& \doteq 7.8
\end{aligned}
$$

The measure of ST is about 7.8 cm .

PTS: 1 DIF: Difficult REF: 1.5 The Pythagorean Theorem
LOC: 8.N1|8.SS1 TOP: Number | Shape and Space (Measurement)
KEY: Communication | Problem-solving Skills
124. ANS:
$9^{2}+12^{2}=15^{2}$
$81+144=225$
$225=225$
Since $225=225$, triangle ABC is a right triangle.

PTS: 1 DIF: Difficult REF: 1.6 Exploring the Pythagorean Theorem
LOC: 8.SS1 TOP: Shape and Space (Measurement)
KEY: Communication | Problem-solving Skills
125. ANS:

Methods may vary. Sample:
$\triangle \mathrm{ABD}$ is a right triangle.

$$
\begin{aligned}
\mathrm{AD}^{2}+\mathrm{BD}^{2} & =\mathrm{AB}^{2} \\
4^{2}+\mathrm{BD}^{2} & =7^{2} \\
\mathrm{BD}^{2} & =7^{2}-4^{2} \\
& =33
\end{aligned}
$$

$\triangle \mathrm{BCD}$ is a right triangle.
$\mathrm{BC}^{2}=\mathrm{BD}^{2}+\mathrm{CD}^{2}$
$\mathrm{BC}^{2}=33+10^{2}$
$\mathrm{BC}^{2}=33+100$
$=133$
$\mathrm{BC}=\sqrt{133}$

$$
\doteq 11.5
$$

The length of BC is about 11.5 cm .

PTS: 1 DIF: Difficult REF: 1.7 Applying the Pythagorean Theorem
LOC: 8.SS1 TOP: Shape and Space (Measurement)
KEY: Communication | Problem-solving Skills
126. ANS:

The sign of the product $(-8)(+9)(+7)(-4)$ is positive.
Explanations may vary. Sample:
There are 2 negative factors in the product. Their product is positive.
The product of any number of positive integers is always positive.
So, the sign of the product $(-8)(+9)(+7)(-4)$ is positive.

PTS: 1 DIF: Difficult REF: 2.2 Developing Rules to Multiply Integers
LOC: 8.N7 TOP: Number KEY: Communication | Problem-solving Skills
127. ANS:

Factors of 22 are: 1, 2, 11, 22
The integers that divide -22 exactly are: $-1,-2,-11,-22,+1,+2,+11,+22$
$\begin{array}{lll}\text { PTS: } 1 & \text { DIF: Difficult } & \text { REF: } 2.4 \text { Developing Rules to Divide Integers } \\ \text { LOC: 8.N7 } & \text { TOP: Number } & \text { KEY: Communication | Problem-solving Skills }\end{array}$
128. ANS:
a) Jamie: $3 \times(+6)+4 \times(+7)+3 \times(-8)$

$$
\begin{aligned}
& =(+18)+(+28)+(-24) \\
& =22
\end{aligned}
$$

Corinne: $5 \times(+6)+2 \times(+7)+3 \times(-8)$
$=(+30)+(+14)+(-24)$
$=20$
b) Since $22>20$, Jamie won.

PTS: 1 DIF: Difficult REF: 2.5 Order of Operations with Integers
LOC: 8.N7
TOP: Number
KEY: Communication | Problem-solving Skills
129. ANS:

$$
\begin{aligned}
4 \frac{4}{5} \times 6 \frac{1}{4} \times \frac{7}{20} & =\frac{24}{5} \times \frac{25}{4} \times \frac{7}{20} \\
& =\frac{24 \times 25 \times 7}{5 \times 4 \times 20}
\end{aligned}
$$

Divide the numerator and denominator by common factors.
$\frac{24 \times 25 \times 7}{5 \times 4 \times 20}=10 \frac{1}{2}$
PTS: 1 DIF: Difficult REF: 3.4 Multiplying Mixed Numbers
LOC: 8.N6 TOP: Number KEY: Communication
130. ANS:
$\sqrt{5 \frac{1}{4} \div 1 \frac{5}{7}}$
$=\sqrt{\frac{21}{4} \div \frac{12}{7}}$
$=\sqrt{\frac{21}{4} \times \frac{7}{12}}$
$=\sqrt{\frac{147}{48}}$
$=\sqrt{\frac{49}{16}}$
$=\frac{7}{4}$
$=1 \frac{3}{4}$

PTS: 1 DIF: Difficult REF: 3.7 Dividing Mixed Numbers
LOC: 8.N6 TOP: Number KEY: Procedural Knowledge | Communication
131. ANS:

Surface area of cylinder $=2 \pi r^{2}+2 \pi r h$

$$
\begin{aligned}
& =2 \pi \times 3^{2}+2 \pi \times 3 \times 8 \\
& =207
\end{aligned}
$$

Surface area of cube $=6 s^{2}$

$$
\begin{aligned}
& =6 \times 6^{2} \\
& =216
\end{aligned}
$$

The cube has the greater surface area.
PTS: 1
LOC: 8.SS3
DIF: Moderate REF: 4.7 Surface Area of a Right Cylinder
TOP: Shape and Space (Measurement) KEY: Communication
132. ANS:

Methods may vary. Sample:
Percent of vaccinated children at risk:
$100 \%-99.75 \%=0.25 \%$
Number of children at risk: $\frac{0.25}{100} \times 564000=1410$
About 1410 children are still at risk of being infected by the virus.
PTS: 1 DIF: Difficult REF: 5.2 Calculating Percents
LOC: 8.N3 TOP: Number KEY: Communication | Problem-solving Skills
133. ANS:

Methods may vary. Sample:
The ratio of red cubes to green cubes is 6:7.
So, the ratio of red cubes to total number of cubes (red plus green) is 6:13.
For every 13 cubes, 6 are red and 7 are green.
Since $234=13 \times 18$, multiply each of 6 and 7 by 18 .
$6 \times 18=108$
$7 \times 18=126$
There are 108 red cubes and 126 green cubes in the bag.
PTS: 1 DIF: Difficult REF: 5.5 Exploring Ratios
LOC: 8.N5 TOP: Number KEY: Communication | Problem-solving Skills
134. ANS:

Store B offers the best buy.
A: Each bottle costs $\$ 2.08$.
B: Each bottle costs $\$ 2.06$.
C: Each bottle costs $\$ 2.07$.
PTS: 1 DIF: Moderate REF: 5.9 Exploring Rates
LOC: 8.N5 TOP: Number KEY: Communication
135. ANS:

Answers may vary. Sample:
Write the equation represented by the balance-scales model.
$x+x+2=x+3+4$
Remove $x$ from each side.
$x+2=3+4$
$x+2=7$
Remove 2 from each side.
$x+2-2=7-2$

$$
x=5
$$

PTS: 1 DIF: Difficult REF: 6.1 Solving Equations Using Models
LOC: 8.PR2 TOP: Patterns and Relations (Variables and Equations)
KEY: Procedural Knowledge | Communication
136. ANS:
a) Graphs may vary. Sample:

b) The ordered pair $(3,5)$ is in both relations.

PTS: 1 DIF: Difficult REF: 6.7 Graphing Linear Relations
LOC: 8.PR1 TOP: Patterns and Relations (Patterns)
KEY: Communication | Problem-solving Skills
137. ANS:
a) $\mathrm{P}(\mathrm{A})=\frac{1}{5}$
$\mathrm{P}($ first 3 A$)=\mathrm{P}(\mathrm{A}) \times \mathrm{P}(\mathrm{A}) \times \mathrm{P}(\mathrm{A})=\frac{1}{5} \times \frac{1}{5} \times \frac{1}{5}=\frac{1}{125}$
b) $\mathrm{P}(\mathrm{B})=\frac{3}{10}$
$P(D)=\frac{7}{20}$
$P(B$, then $D 2$ times $)=P(B) \times P(D) \times P(D)=\frac{3}{10} \times \frac{7}{20} \times \frac{7}{20}=\frac{147}{4000}$
c) $\mathrm{P}(\operatorname{not} \mathrm{A})=\frac{4}{5}$
$\mathrm{P}($ not A 3 times $)=\mathrm{P}($ not A$) \times \mathrm{P}(\operatorname{not} \mathrm{A}) \times \mathrm{P}(\operatorname{not} \mathrm{A})=\frac{4}{5} \times \frac{4}{5} \times \frac{4}{5}=\frac{64}{125}$

PTS: 1
DIF: Difficult REF: 7.4 Solving Problems Involving Independent Events
LOC: 8.SP2 TOP: Statistics and Probability (Chance and Uncertainty)
KEY: Communication | Problem-solving Skills
138. ANS:

Shape B is the image of Shape A after a reflection in the diagonal Line $m$.


PTS: 1 DIF: Difficult REF: 8.4 Identifying Transformations
LOC: 8.SS6 TOP: Shape and Space (Transformations)
KEY: Procedural Knowledge | Problem-solving Skills
139. ANS:

Answers may vary. Sample:

- Translation 4 units right followed by reflection in the horizontal line through 6 on the vertical axis
- $90^{\circ}$ clockwise rotation about point $(8,4)$ followed by $90^{\circ}$ clockwise rotation about point $(10,6)$
- Reflection in the horizontal line through 6 on the vertical axis followed by reflection in the vertical line through 8 on the horizontal axis

PTS: 1 DIF: Difficult REF: 8.6 Identifying Transformations in Tessellations
LOC: 8.SS6 TOP: Shape and Space (Transformations)
KEY: Communication | Problem-solving Skills

